CS 51 Code Review 4

Modules and Functors in OCaml

Sam Green and Gabbi Merz

Harvard University

- 1. Modules and Abstraction
- 2. Functors
- 3. Binary Heaps (for Ps4)

Modules and Abstraction

- A **module** is a collection of values (and remember, functions are values) and types.
- A module signature or module type describes the contents of a module.
- While not precisely true, this analogy may help:

 $\frac{\texttt{type}}{\texttt{value}} \cong \frac{\texttt{signature}}{\texttt{module}}$

Modules

Here's a definition of the Math module:

```
# module Math =
    struct
        let pi = 3.14159
        let cos = cos
        let \sin = \sin
        let sum = (+.)
        let max (lst : float list) =
          match 1st with
          | | -> None
          | hd :: tl -> Some (List.fold_right max tl hd)
    end ;;
```

Important syntax here: module, struct, end. What are these for? Are they analogous to other syntax we've seen so far?

Module Signatures

The type analog for modules is the module signature. For example:

```
# module type TF =
sig
type info
val info : info
val hometown : string
val print_info : unit -> unit
val grade_assignment : int -> string
val favorite_function : float -> float -> float
val fold : int list -> int -> int
end ;;
```

We could then apply this signature to the Sam or Gabbi module. (Remember, files are module by default!)

```
module TFGabbi = Gabbi : TF ;;
```

A BigNum Module.

What happened when you typed #mod_use ''ps3.ml'' into utop while you were working on problem set 3?

```
Something like this (output omitted for space):
```

```
module Ps3 :
    sig
    type bignum = { neg : bool; coeffs : int list; }
    val base : int
    val negate : bignum -> bignum
    val equal : bignum -> bignum -> bool
...
```

(Notice that Ps3 has an anonymous module signature applied to it! This signature is the default, which exposes every defined type and values. It's inferred automatically by the compiler!)

What are some undesirable design properties of this default?

The solution to these problems is to write a module signature and use it to enforce an abstraction barrier between client code and the Ps3 module.

Let's imagine that the only values we wanted to include were toInt, fromInt, plus, negate, and times. What would the signature be? How would we create a BigNum module out of this signature and the Ps3 module?

Functors

Informally, a **functor** is a "function" from modules to modules. More precisely, a functor is a module that is **parameterized** by another module. Some possible uses:

- Enforce abstractions.
- Make code more generic.
- Make code more extensible.

Imagine we needed a stack data structure as part of a system we were building. What's the "simplest" way to use the following signature for stacks with elements of several different types?

```
# module type STACK =
  sig
    exception Empty
    type element
   type stack
    val empty : unit -> stack
    val push : element -> stack -> stack
    val top : stack -> element
    val pop : stack -> stack
    val serialize : stack -> string
  end ::
```

```
module type SERIALIZE =
  sig
    type t
    val serialize : t -> string
  end ;;
module MakeStack (Element: SERIALIZE)
    : (STACK with type element = Element.t) =
    struct
    type element = Element.t ;;
    . . .
    end ;;
```

Create a module to handle stacks of (int, int) values.

Imagine we have a module that implements this signature:

```
# module type X_int =
    sig
    val x : int
    end ;;
```

How can we write a functor that takes a module of type X_int and create a new module of type X_int with the value x incremented?

¹Thanks to Niamh Mulholland!

Binary Heaps (for Ps4)

The conceptual idea for this week's problem set is about modules and functors. It's also the first foray into a real abstraction.

The motivating problem is a priority queue. The implementation progression is:

- 1. List based.
- 2. Binary search tree based.
- 3. Binary heap based.

The binary heap implementation allows for $O(\log n)$ operations that could be worst case O(n) in other implementations.

A binary (min)heap is a binary search tree that satisfies additional representation invariants.²

The first is an ordering invariant:

The value stored at the root of any subtree (including the root of the whole tree) must be smaller than all values stored in the subtrees below the root.

The second is a **balance** invariant:

For any node, its left child tree is either the same size as (in number of nodes) or exactly one node larger than its right child tree.

²Recall the definition of representation invariant!

The biggest challenge in implementing the binary heap is understanding the rules for inserting and popping so that these invariants are enforced. So let's this sequence of operations to get comfortable:

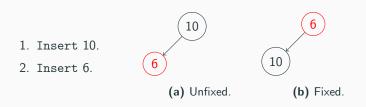
- 1. Insert 10.
- 2. Insert 6.
- 3. Insert 6.
- 4. Insert 5.
- 5. Insert 11.
- 6. Insert 1.
- 7. Take.

1. Insert 10.



- 1. Insert 10.
- 2. Insert 6.



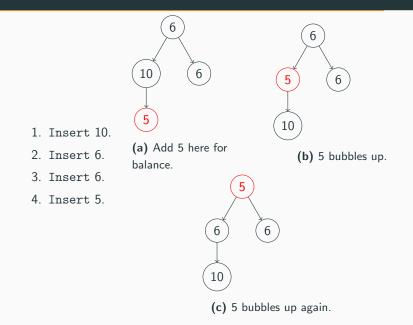


- 1. Insert 10.
- 2. Insert 6.
- 3. Insert 6.

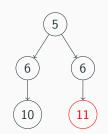


No fix required.

Add a 5

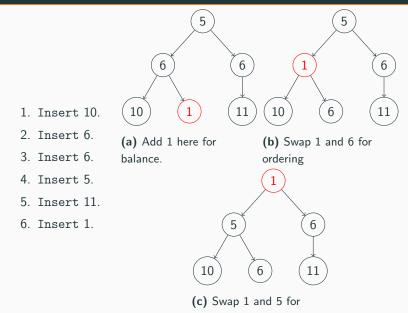


- 1. Insert 10.
- 2. Insert 6.
- 3. Insert 6.
- 4. Insert 5.
- 5. Insert 11.



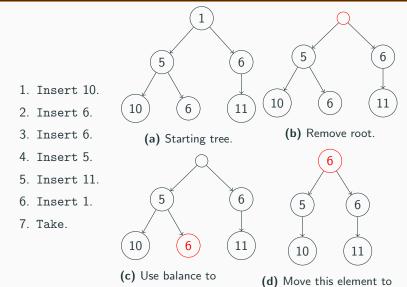
Add 11 here for balance, no fix required.

$\mathsf{Add}\ \mathsf{a}\ 1$



ordering

Take the Lowest Element.



identify element to move. the top, then fix.

- 1. Understand the invariants.
- 2. Enforce the invariants separately.
- 3. Identify the recursive structure. Note that invariant properties apply to subtrees! (Hint.)
- 4. Draw pictures.
- 5. (Try not to code until you understand the data structure)

Questions? Remember to fill out the form! http://sa.muel.green/cs51